

Short Note

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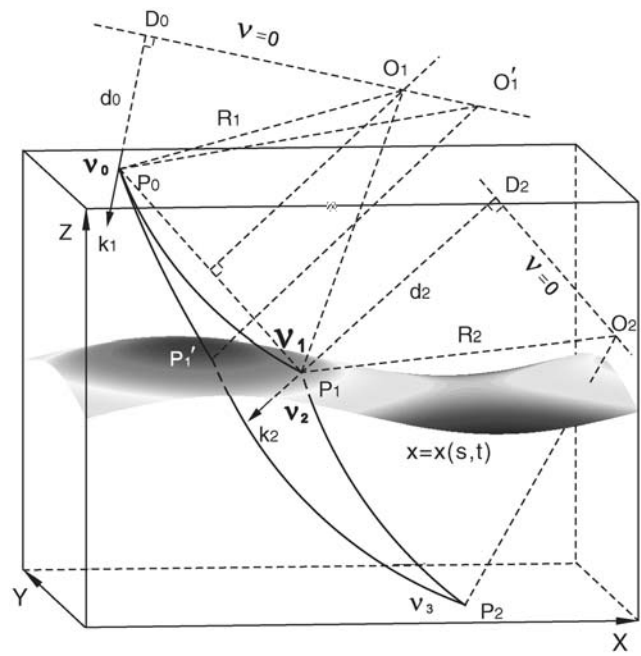
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r - m r m r f r r r r m r



$\mathbf{r} = (x, y, z)$  is the position vector of a point in the fluid. The velocity vector  $\mathbf{v}$  is decomposed into a mean velocity  $\mathbf{v}_0$  and a fluctuating velocity  $\mathbf{v}'$ . The mean velocity is assumed to be a function of the mean position  $\mathbf{r}_0$  and time  $t$ . The fluctuating velocity is assumed to be a function of the fluctuating position  $\mathbf{r}'$  and time  $t$ . The mean position is defined as  $\mathbf{r}_0 = \langle \mathbf{r} \rangle$  and the fluctuating position is defined as  $\mathbf{r}' = \mathbf{r} - \mathbf{r}_0$ . The mean velocity is given by  $\mathbf{v}_0 = \langle \mathbf{v} \rangle$  and the fluctuating velocity is given by  $\mathbf{v}' = \mathbf{v} - \mathbf{v}_0$ . The mean velocity is assumed to be a function of the mean position  $\mathbf{r}_0$  and time  $t$ . The fluctuating velocity is assumed to be a function of the fluctuating position  $\mathbf{r}'$  and time  $t$ . The mean position is defined as  $\mathbf{r}_0 = \langle \mathbf{r} \rangle$  and the fluctuating position is defined as  $\mathbf{r}' = \mathbf{r} - \mathbf{r}_0$ . The mean velocity is given by  $\mathbf{v}_0 = \langle \mathbf{v} \rangle$  and the fluctuating velocity is given by  $\mathbf{v}' = \mathbf{v} - \mathbf{v}_0$ .



**Fig. 1.** Control volume in a fluid flow. The surface  $x=x(s,t)$  is the mean position of the control volume. The points  $P_0, P_1, P_2$  are the points on the surface. The velocity vectors  $\mathbf{v}_0, \mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3$  are the mean velocity vectors at these points. The points  $O_1, O_1', O_2, O_2'$  are the points on the top and bottom surfaces. The distances  $d_0, d_2$  are the distances from the surface to the top and bottom surfaces. The condition  $v=0$  is noted at the top and right boundaries.

$$\left. \frac{\partial T}{\partial s} \right|_{(s=\xi+\Delta s, t=\eta+\Delta t)} = 0, \quad \left. \frac{\partial T}{\partial t} \right|_{(s=\xi+\Delta s, t=\eta+\Delta t)} = 0. \quad (1)$$

$$\begin{aligned} \frac{\partial T}{\partial x_i} x_{is} + \left( \frac{\partial^2 T}{\partial x_i \partial x_j} x_{is} x_{js} + \frac{\partial T}{\partial x_i} x_{iss} \right) \Delta s \\ + \left( \frac{\partial^2 T}{\partial x_i \partial x_j} x_{is} x_{jt} + \frac{\partial T}{\partial x_i} x_{ist} \right) \Delta t = 0, \\ \frac{\partial T}{\partial x_i} x_{it} + \left( \frac{\partial^2 T}{\partial x_i \partial x_j} x_{it} x_{js} + \frac{\partial T}{\partial x_i} x_{its} \right) \Delta s \\ + \left( \frac{\partial^2 T}{\partial x_i \partial x_j} x_{it} x_{jt} + \frac{\partial T}{\partial x_i} x_{itt} \right) \Delta t = 0, \end{aligned} \quad (2)$$

The mean position  $\mathbf{x} = \mathbf{x}(s, t)$  is defined as  $\mathbf{x} = \mathbf{x}(s, t)$ .

$$T = t_1(P_0, \mathbf{x}) + t_2(\mathbf{x}, P_2). \quad (3)$$

$$\begin{aligned} \Delta s &= \frac{U_{13}U_{22} - U_{23}U_{12}}{U_{11}U_{22} - U_{12}U_{21}}, \\ \Delta t &= \frac{U_{11}U_{23} - U_{21}U_{13}}{U_{11}U_{22} - U_{12}U_{21}}, \end{aligned} \quad (4)$$

The mean position  $\mathbf{x} = \mathbf{x}(s, t)$  is defined as  $\mathbf{x} = \mathbf{x}(s, t)$ .

$$\begin{aligned}
U_{11} &= \frac{\partial^2 T}{\partial x_i \partial x_j} x_{is} x_{js} + \frac{\partial T}{\partial x_i} x_{iss}, \\
U_{12} &= \frac{\partial^2 T}{\partial x_i \partial x_j} x_{is} x_{jt} + \frac{\partial T}{\partial x_i} x_{ist}, & U_{13} &= -\frac{\partial T}{\partial x_i} x_{is}, \\
U_{21} &= \frac{\partial^2 T}{\partial x_i \partial x_j} x_{it} x_{js} + \frac{\partial T}{\partial x_i} x_{its}, \\
U_{22} &= \frac{\partial^2 T}{\partial x_i \partial x_j} x_{it} x_{jt} + \frac{\partial T}{\partial x_i} x_{itt}, & U_{23} &= -\frac{\partial T}{\partial x_i} x_{it}, \\
x_{is} &= \frac{\partial x_i}{\partial s}, & x_{it} &= \frac{\partial x_i}{\partial t}, & x_{iss} &= \frac{\partial^2 x_i}{\partial s^2}, \\
x_{ist} &= x_{its} = \frac{\partial x_i}{\partial s} \frac{\partial x_i}{\partial t}, & x_{itt} &= \frac{\partial^2 x_i}{\partial t^2}.
\end{aligned} \tag{10}$$

$(\xi, \eta)$   $(\xi + \Delta s, \eta + \Delta t)$   $f(x, y, z) = 0$ ,  $s = x, t = y$ ,

$$\begin{aligned}
x_{1s} &= 1, & x_{2s} &= 0, & x_{3s} &= \frac{\partial z}{\partial x}, \\
x_{1t} &= 0, & x_{2t} &= 1, & x_{3t} &= \frac{\partial z}{\partial y}, \\
x_{iss} &= x_{ist} = x_{its} = x_{itt} = 0, & (i &= 1, 2), \\
x_{3ss} &= \frac{\partial^2 z}{\partial x^2}, & x_{3st} &= x_{3ts} = \frac{\partial^2 z}{\partial x \partial y}, & x_{3tt} &= \frac{\partial^2 z}{\partial y^2}.
\end{aligned} \tag{11}$$

$(n_1, n_2, n_3)$   $2(-\frac{\partial z}{\partial x}, -\frac{\partial z}{\partial y}, 1)$

$$\frac{\partial z}{\partial x} = -\frac{n_1}{n_3}, \quad \frac{\partial z}{\partial y} = -\frac{n_2}{n_3}. \tag{12}$$

$n_3$

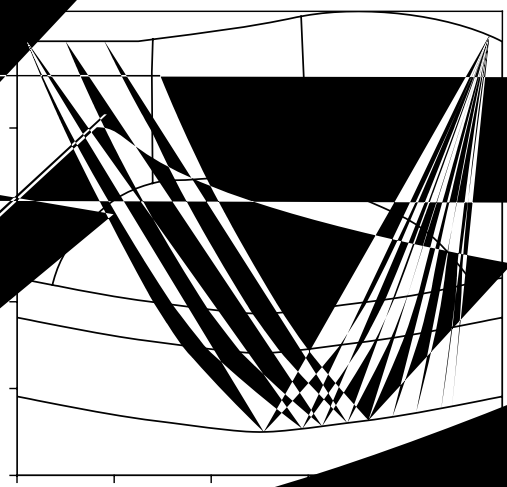
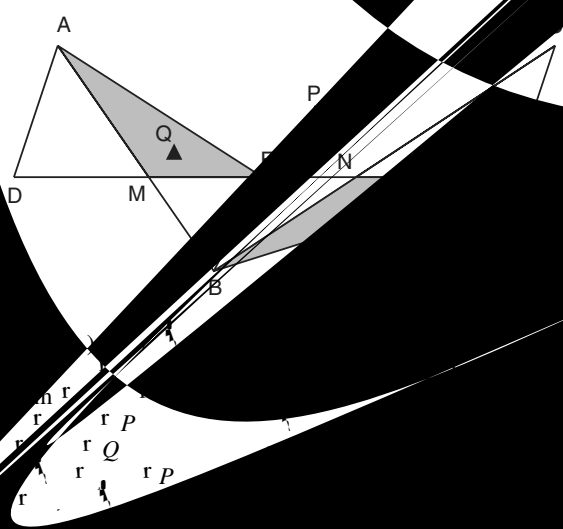
$$\tag{10}$$

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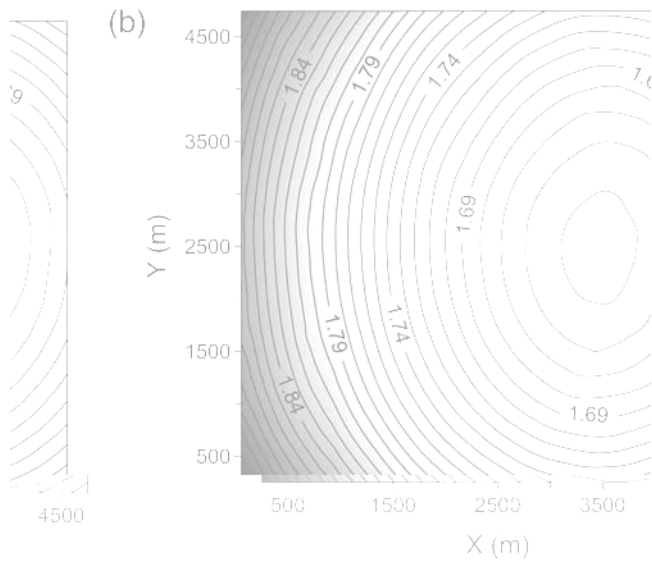
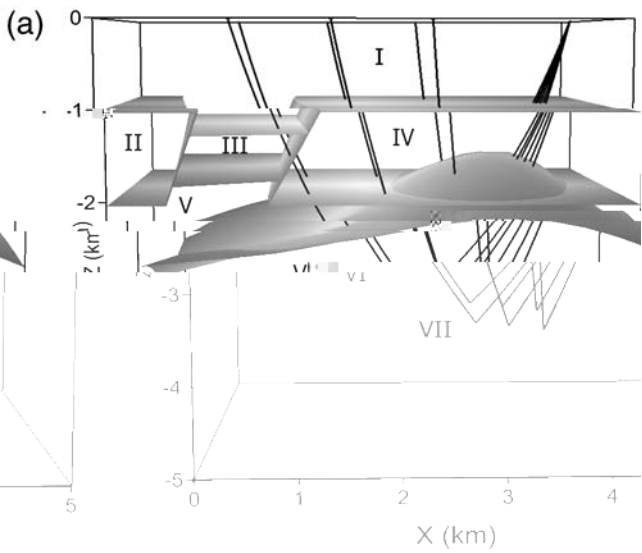
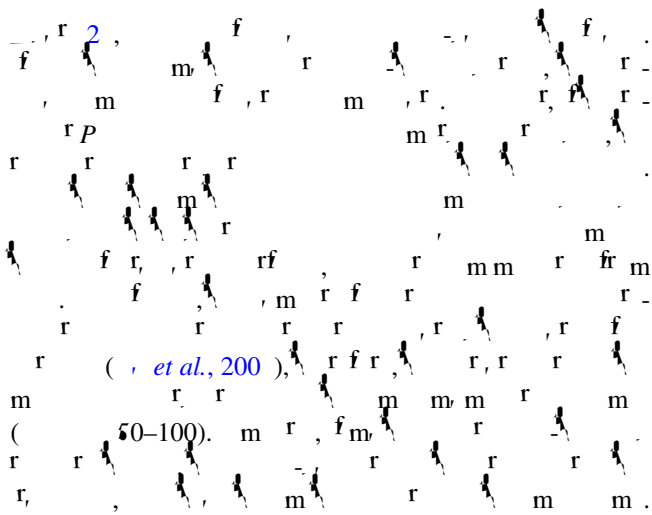


Figure 4. ( ) m r m ( 2) r r r f r r r . ( )

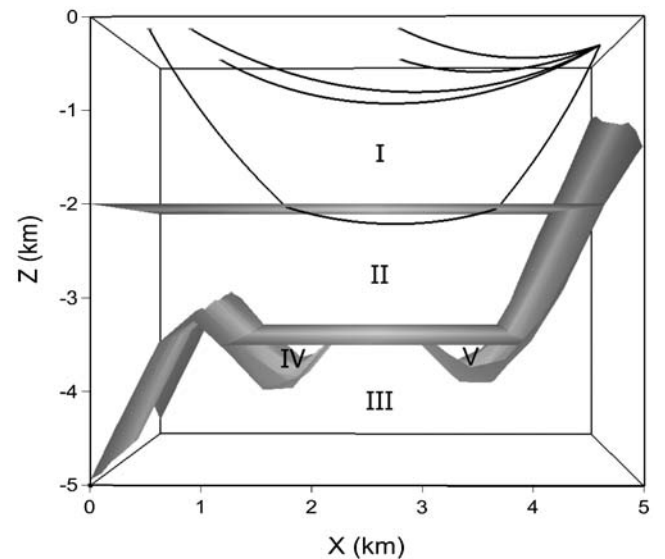
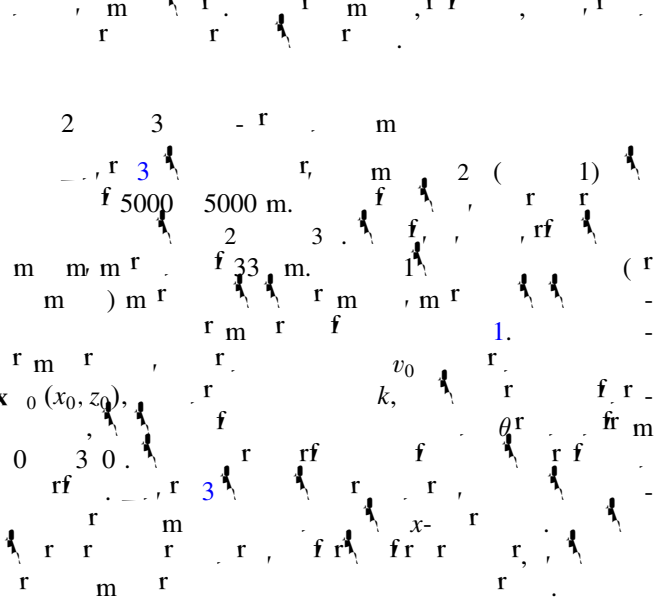
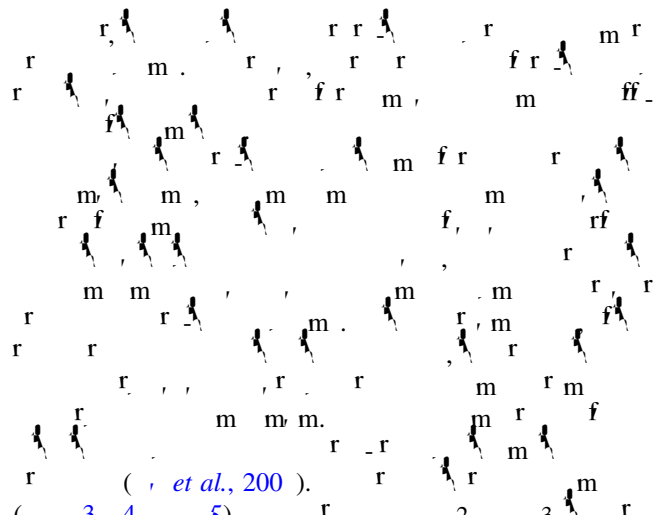


Figure 5. r , m-r , m ( 3) f 4 r r r , f , r

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|-----------|----------|----------|----------|---------|-----------|---------|--|
| $V_0, m/$ | $X_0, m$ | $Y_0, m$ | $Z_0, m$ | $k, -1$ | $\theta,$ | $\phi,$ |  |
| 3000      | 2500     | 2500     | 0        | 0.      | 1 0       | 0       |  |
| 3 00      | 250      | 2500     | -1000    | 0.      | 1 0       | 1 0     |  |
| 4000      | 1250     | 2500     | -1250    | 0.5     | 1 0       | 1 0     |  |
| 3 00      | 3500     | 2500     | -1000    | 0.      | 1 5       | 355     |  |
| 4 00      | 1000     | 2500     | -2000    | 0.5     | 1 5       | 5       |  |
| 5 00      | 2500     | 2500     | -2000    | 0.      | 1 0       | 0       |  |
| 500       | 2500     | 2500     | -3700    | 0.      | 1 0       | 0       |  |

\* 1 f r f f r m r.  $\theta, r$  fr m 0  
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x- y- r - m  
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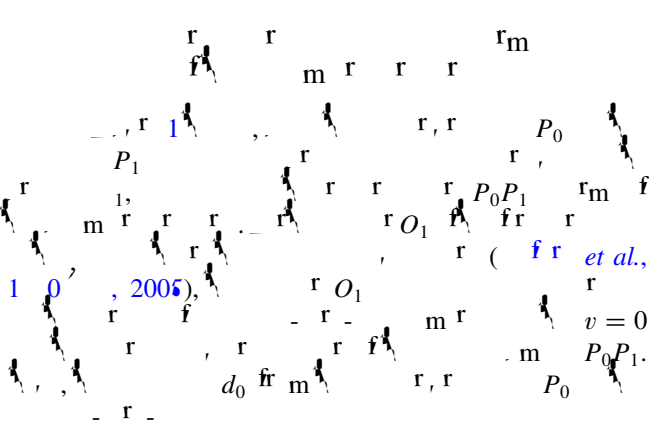
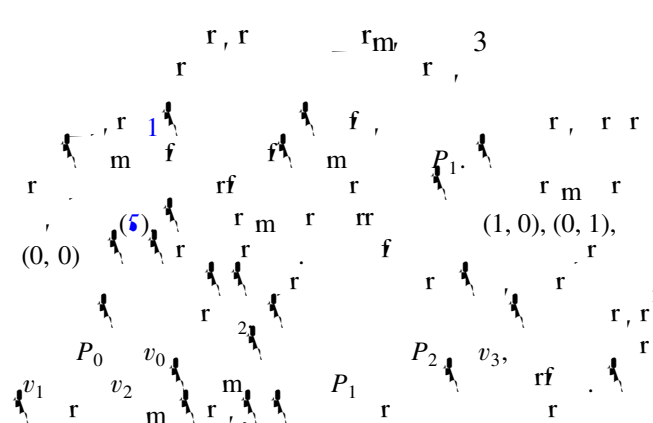
| r , r    |          |          | r * f 2   |     |  |
|----------|----------|----------|-----------|-----|--|
| $X_0, m$ | $Y_0, m$ | $Z_0, m$ | $V_0, m/$ | m r |  |

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$$T = t(P_0, P_1) + t(P_1, P_2) = \frac{1}{k_1} r_1 p_1 + \frac{1}{k_2} r_2 p_2, \quad (1)$$

$$p_1 = 1 + \frac{k_1^2 r_1^2}{2v_1^{(1)}v_2^{(2)}}, \quad (1)$$

$$p_2 = 1 + \frac{k_2^2 r_2^2}{2v_2^{(2)}v_3^{(3)}},$$

$$k_1 = \| \mathbf{x}_1 \|, \quad k_2 = \| \mathbf{x}_2 \|, \quad r_1 = \| \mathbf{x}^{(2)} - \mathbf{x}^{(1)} \|, \quad (2)$$

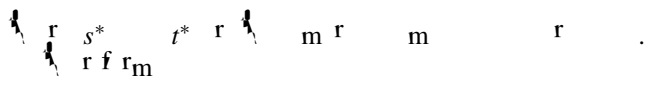
$$r_2 = \| \mathbf{x}^{(2)} - \mathbf{x}^{(3)} \|.$$

$$\frac{\partial T}{\partial s} \Big|_{(s=s^*, t=t^*)} = 0, \quad \frac{\partial T}{\partial t} \Big|_{(s=s^*, t=t^*)} = 0, \quad (3)$$

$$d_0 = \frac{v_0}{k_1}. \quad (1)$$

$$\| \mathbf{O}_1 \mathbf{P}_0 \| = R_1, \quad \| \mathbf{O}_1 \mathbf{P}_1 \| = R_1, \quad \mathbf{P}_0 \mathbf{O}_1 \cdot \mathbf{P}_0 \mathbf{D}_0 = d_0^2, \quad (2)$$

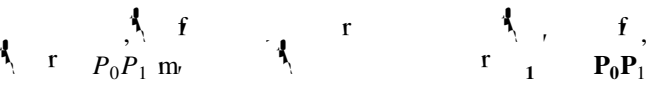
$$\mathbf{O}_1 (\mathbf{O}_1 \mathbf{P}_0 - \mathbf{O}_1 \mathbf{P}_1) = 0.$$



$$\| \mathbf{O}_1 \| = R_1. \quad (3)$$

$$\left( k_2 \sqrt{p_2^2 - 1} \frac{\partial p_1}{\partial s} + k_1 \sqrt{p_1^2 - 1} \frac{\partial p_2}{\partial s} \right) \Big|_{(s=s^*, t=t^*)} = 0,$$

$$\left( k_2 \sqrt{p_2^2 - 1} \frac{\partial p_1}{\partial t} + k_1 \sqrt{p_1^2 - 1} \frac{\partial p_2}{\partial t} \right) \Big|_{(s=s^*, t=t^*)} = 0. \quad (4)$$



$$\mathbf{x}(\mathbf{x}_0) (\mathbf{O}_1 \mathbf{P}_0 \mathbf{P}_1) = 0. \quad (4)$$



$$\begin{aligned} & \sqrt{p_1^2 - 1} \Big|_{(s=s^*, t=t^*)} \\ &= \sqrt{p_1^2 - 1} + \frac{p_1}{\sqrt{p_1^2 - 1}} \frac{\partial p_1}{\partial x_i} (x_{is} \Delta s + x_{it} \Delta t), \\ & \frac{\partial p_1}{\partial s} \Big|_{(s=s^*, t=t^*)} \\ &= \frac{\partial p_1}{\partial x_i} x_{is} + \left( \frac{\partial^2 p_1}{\partial x_i \partial x_j} x_{is} x_{js} + \frac{\partial p_1}{\partial x_i} x_{iss} \right) \Delta s \\ & \quad + \left( \frac{\partial^2 p_1}{\partial x_i \partial x_j} x_{is} x_{jt} + \frac{\partial p_1}{\partial x_i} x_{ist} \right) \Delta t. \end{aligned} \quad (5)$$

$$\Delta s = \frac{U_{13} U_{22} - U_{23} U_{12}}{U_{11} U_{22} - U_{12} U_{21}}, \quad \Delta t = \frac{U_{11} U_{23} - U_{21} U_{13}}{U_{11} U_{22} - U_{12} U_{21}}, \quad (4)$$

$$U_{11} = k_2 (e_2 A_s^{(1)} A_s^{(3)} + f_2 B_{ss}^{(1)}) + k_1 (e_1 A_s^{(1)} A_s^{(3)} + f_1 B_{ss}^{(3)}),$$

$$U_{12} = k_2 (e_2 A_s^{(1)} A_t^{(3)} + f_2 B_{st}^{(1)}) + k_1 (e_1 A_t^{(1)} A_s^{(3)} + f_1 B_{st}^{(3)}),$$

$$U_{13} = -(k_2 f_2 A_s^{(1)} + k_1 f_1 A_s^{(3)}),$$

$$U_{21} = k_2 (e_2 A_t^{(1)} A_s^{(3)} + f_2 C_{ts}^{(1)}) + k_1 (e_1 A_s^{(1)} A_t^{(3)} + f_1 C_{ts}^{(3)}),$$

$$U_{22} = k_2 (e_2 A_t^{(1)} A_t^{(3)} + f_2 C_{tt}^{(1)}) + k_1 (e_1 A_t^{(1)} A_t^{(3)} + f_1 C_{tt}^{(3)}),$$

$$U_{23} = -(k_2 f_2 A_t^{(1)} + k_1 f_1 A_t^{(3)}), \quad e_1 = \frac{p_1}{\sqrt{p_1^2 - 1}},$$

$$e_2 = \frac{p_2}{\sqrt{p_2^2 - 1}}, \quad f_1 = \sqrt{p_1^2 - 1}, \quad f_2 = \sqrt{p_2^2 - 1},$$

$$A_s^{(1)} = Q_i^{(1)} x_{is}^{(2)}, \quad A_t^{(1)} = Q_i^{(1)} x_{it}^{(2)}, \quad A_s^{(3)} = Q_i^{(3)} x_{is}^{(2)},$$

$$A_t^{(3)} = Q_i^{(3)} x_{it}^{(2)}, \quad B_{ss}^{(1)} = Q_i^{(1)} x_{iss}^{(2)} + R_{ij}^{(1)} x_{is}^{(2)} x_{js}^{(2)},$$

$$B_{st}^{(1)} = Q_i^{(1)} x_{ist}^{(2)} + R_{ij}^{(1)} x_{is}^{(2)} x_{jt}^{(2)},$$

$$B_{ss}^{(3)} = Q_i^{(3)} x_{iss}^{(2)} + R_{ij}^{(3)} x_{is}^{(2)} x_{js}^{(2)},$$

$$B_{st}^{(3)} = Q_i^{(3)} x_{ist}^{(2)} + R_{ij}^{(3)} x_{is}^{(2)} x_{jt}^{(2)},$$

$$C_{ts}^{(1)} = Q_i^{(1)} x_{its}^{(2)} + R_{ij}^{(1)} x_{it}^{(2)} x_{js}^{(2)},$$

$$C_{tt}^{(1)} = Q_i^{(1)} x_{itt}^{(2)} + R_{ij}^{(1)} x_{it}^{(2)} x_{jt}^{(2)},$$

$$C_{ts}^{(3)} = Q_i^{(3)} x_{its}^{(2)} + R_{ij}^{(3)} x_{it}^{(2)} x_{js}^{(2)},$$

$$C_{tt}^{(3)} = Q_i^{(3)} x_{itt}^{(2)} + R_{ij}^{(3)} x_{it}^{(2)} x_{jt}^{(2)},$$

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$$Q_i^{(1)} = \frac{k_1^2}{2v_0} \frac{2(x_i^{(2)} - x_i^{(1)})v_1 - r_1^2 k_i^{(1)}}{v_1^2},$$

$$Q_i^{(3)} = \frac{k_2^2}{2v_3} \frac{2(x_i^{(2)} - x_i^{(3)})v_2 - r_2^2 k_i^{(2)}}{v_2^2},$$

$$R_{ij}^{(1)} = \frac{k_1^2}{v_0} \left( \frac{\delta_{ij} v_1 - (x_i^{(2)} - x_i^{(1)}) k_j^{(1)} - (x_j^{(2)} - x_j^{(1)}) k_i^{(1)}}{v_1^2} + \frac{r_1^2 k_i^{(1)} k_j^{(1)}}{v_1^3} \right),$$

$$R_{ij}^{(3)} = \frac{k_2^2}{v_3} \left( \frac{\delta_{ij} v_2 - (x_i^{(2)} - x_i^{(3)}) k_j^{(2)} - (x_j^{(2)} - x_j^{(3)}) k_i^{(2)}}{v_2^2} + \frac{r_2^2 k_i^{(2)} k_j^{(2)}}{v_2^3} \right),$$

$$k_i^{(1)} = v_1, \quad k_i^{(2)} = v_2, \quad v_0 = v_1^{(1)},$$

$$v_1 = v_1^{(2)}, \quad v_2 = v_2^{(2)}, \quad v_3 = v_3^{(3)},$$

$$\delta_{ij} = \begin{cases} 1, & i = j \\ 0, & i \neq j \end{cases}, \quad x_{is}^{(2)} = \frac{\partial x_i^{(2)}}{\partial s}, \quad x_{it}^{(2)} = \frac{\partial x_i^{(2)}}{\partial t},$$

$$x_{iss}^{(2)} = \frac{\partial^2 x_i^{(2)}}{\partial s^2}, \quad x_{ist}^{(2)} = x_{its}^{(2)} = \frac{\partial^2 x_i^{(2)}}{\partial s \partial t},$$

$$x_{itt}^{(2)} = \frac{\partial^2 x_i^{(2)}}{\partial t^2} \quad ( )$$

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